

NCSX Flux Surfaces

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for the NCSX Magnetic Surface Group

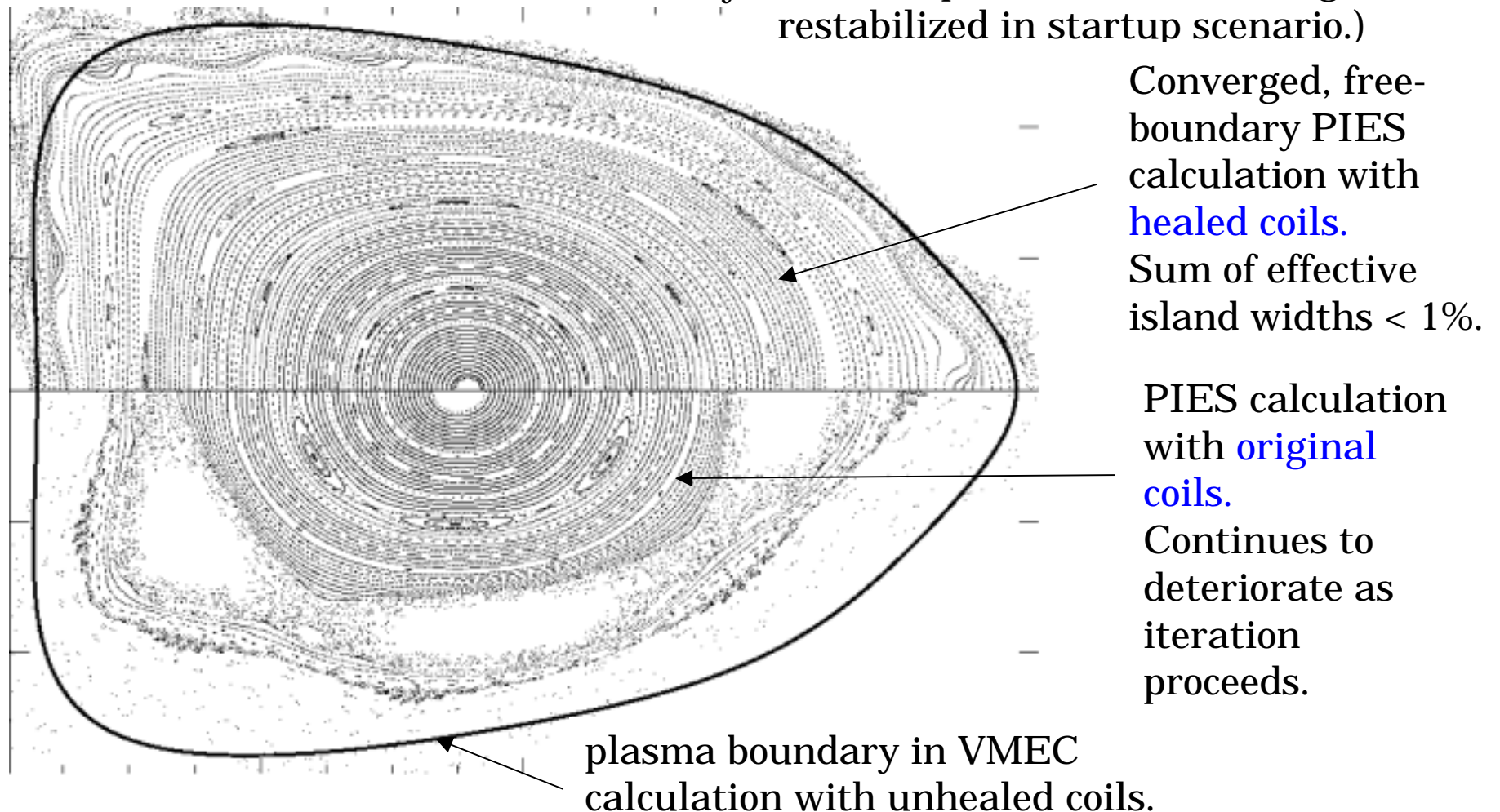
NCSX Conceptual Design Review
Princeton, NJ
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NCSX is Designed to Have Good Flux Surfaces

- NCSX coils designed to produce good flux surfaces. (PIES code)
- NCSX designed so that neoclassical effects reduce island widths.
- Have verified that coils give acceptable surfaces for range of configurations.
 - Equilibrium calculations with PIES code. (Do not include neoclassical effects.)
 - Estimate neoclassical effect and effect of finite $\chi_{\perp} / \chi_{\parallel}$ in assessing effective total surface loss.
- External and internal trim coils designed to extend range of configurations with good surfaces.
- Strong ambipolar flow predicted to shield out resonant perturbations.

Coil Design Has Been Modified to Produce Good Surfaces

- “Dynamic healing” algorithm modifies coils in each PIES iteration to suppress targeted islands.
- Preserves engineering and physics constraints on coil curvature, minimum distance between coils, kink stability. (Stable up to $n=45$. Ballooning restabilized in startup scenario.)



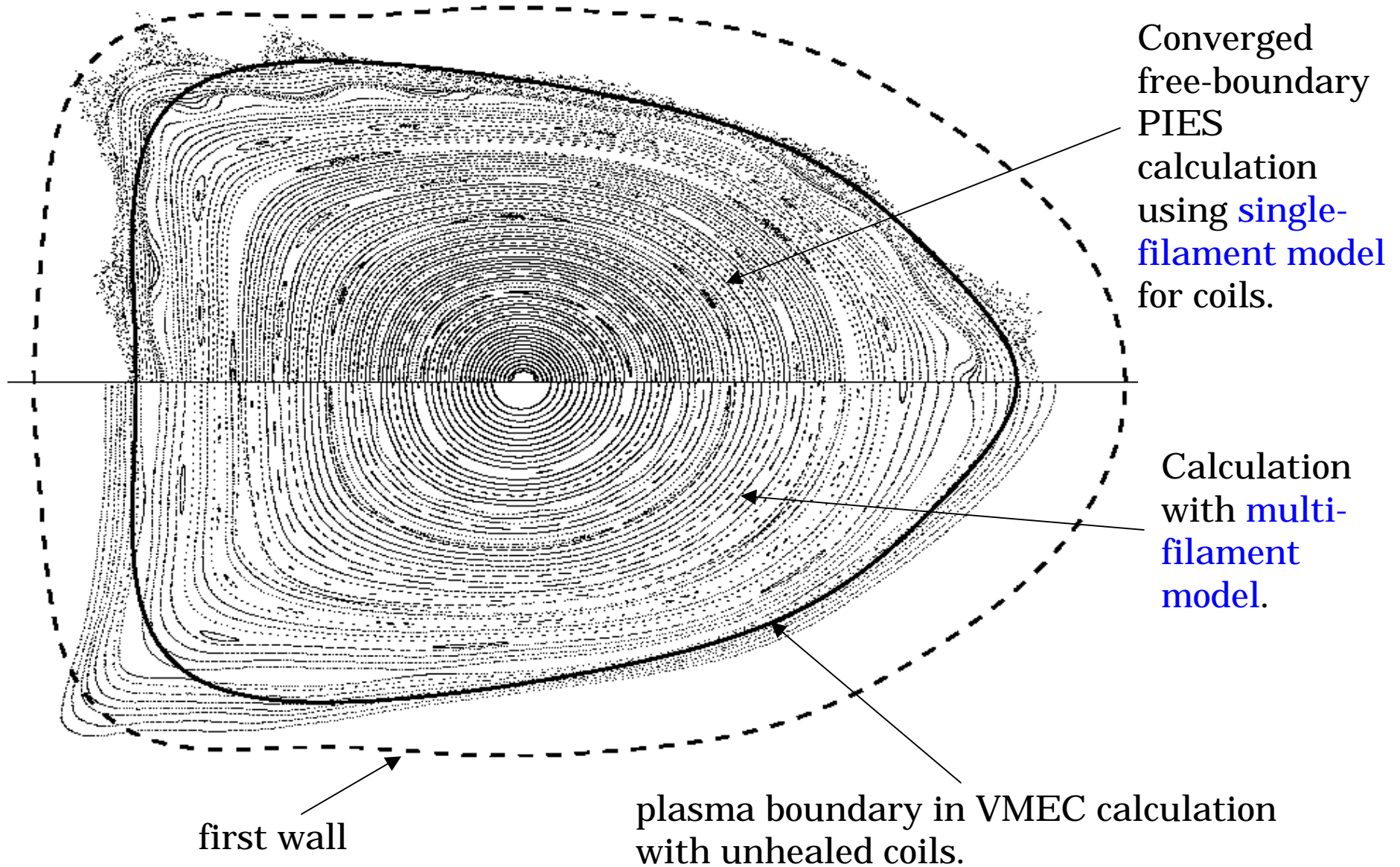
Small Islands Have Little Effect on Transport

- Large islands short-circuit confinement by allowing heat to flow along separatrix.



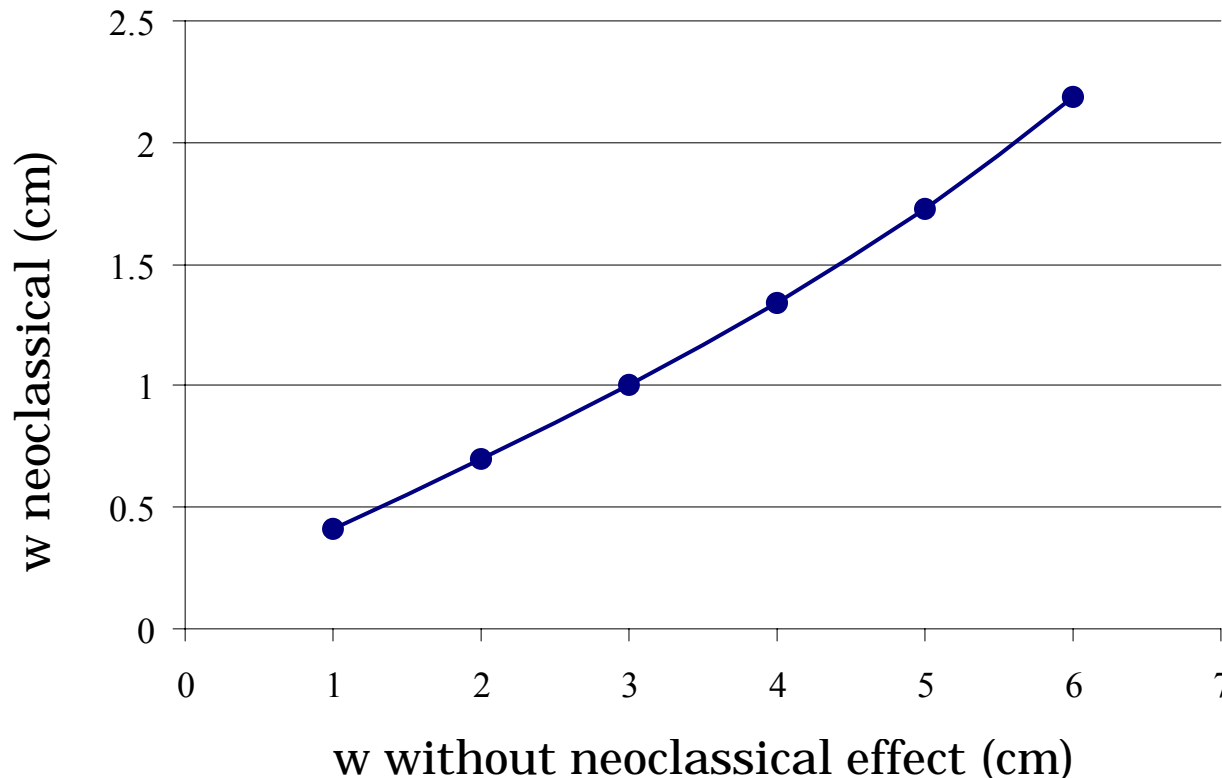
- For narrow islands, path length along field line long, and parallel conductivity prevents short-circuiting of confinement.
- Critical island width at which transport due to island is comparable to cross-field transport: $w_0 \approx 5 (\chi_{\perp} / \chi_{\parallel})^{0.25} (RL_{\perp} / m\tau)^{0.5}$, where L_{\perp} is shear scale length.
- Estimate $w_0/a \approx 3.5\%$ for $m=5$ island in NCSX. (At $\beta = 4.2\%$, $B = 1.2$ T, $\langle n_e \rangle = 5.8 \times 10^{19} \text{ m}^{-3}$)
- In calculating flux surface loss, use effective island width $w/(1+(w_0/w)^4)$.
(Effective diffusivity across island $\chi \approx \chi_{\perp} (1+(w/w_0)^4)$).

Multi-Filament Model Improves Flux Surfaces



Neoclassical Effect Reduces Island Widths in NCSX

- Gives neoclassical tearing mode in tokamaks ($\iota' < 0$).
- For $\iota' > 0$, effect predicted to reduce NCSX island widths.



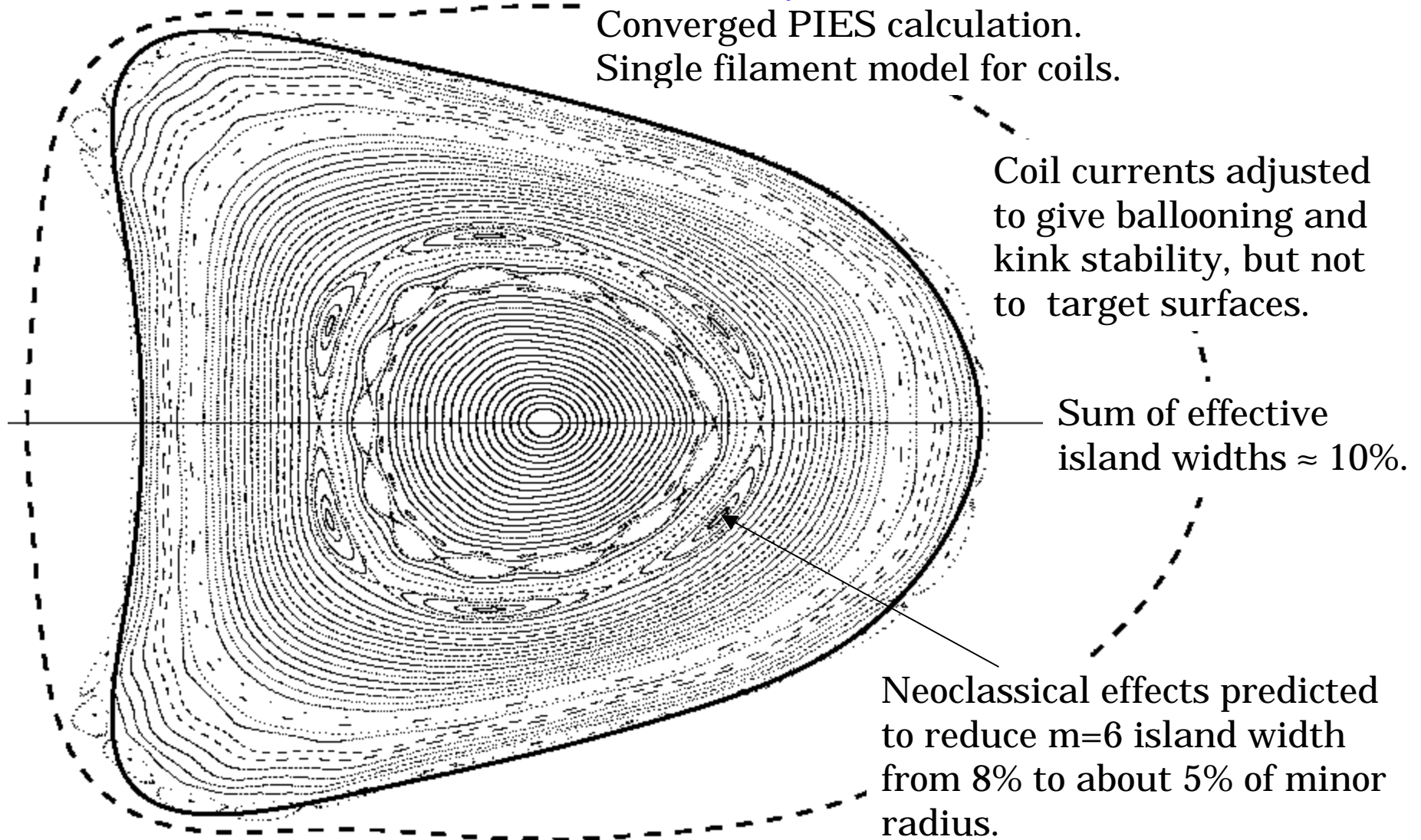
Effect estimated for island at $\iota = 0.6$ surface. Analytic calculation in cylinder. Estimate $\Delta' = -2 \text{ m} / \text{r}$. Take $\beta = 4.2\%$, $B = 1.2 \text{ T}$, $\langle n_e \rangle = 5.8 \times 10^{19} \text{ m}^{-3}$.

- Evaluation of effective island widths takes into account finite $\chi_{\perp} / \chi_{\parallel}$ effect, as well as neoclassical effect.

Flux Surfaces Evaluated for Five Snapshots in Startup Scenario are Acceptable

$t = 100 \text{ ms}$, $\beta = 3.4\%$

Converged PIES calculation.
Single filament model for coils.



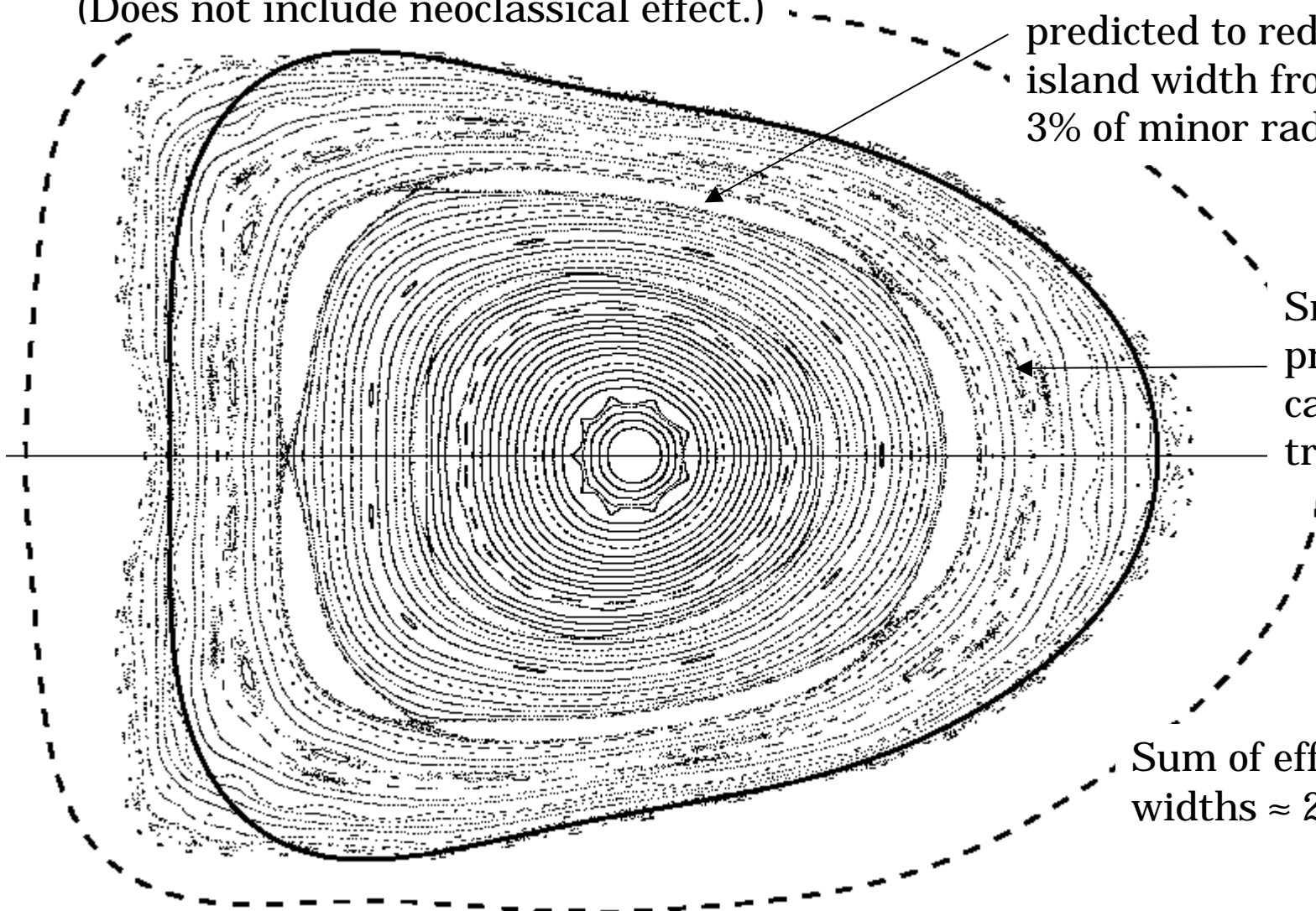
Good Flux Surfaces at β Values Exceeding Design Value, with Transport Determined Profiles

$t = 303$ ms, $\beta = 4.6\%$. Converged
PIES calculation with healed coils.
(Does not include neoclassical effect.)

Neoclassical effect
predicted to reduce $m=5$
island width from 6% to
3% of minor radius.

Small islands
predicted to
cause little
transport.

Sum of effective island
widths $\approx 2.5\%$.



Summary of Effective Flux Surface Loss for PIES Calculations

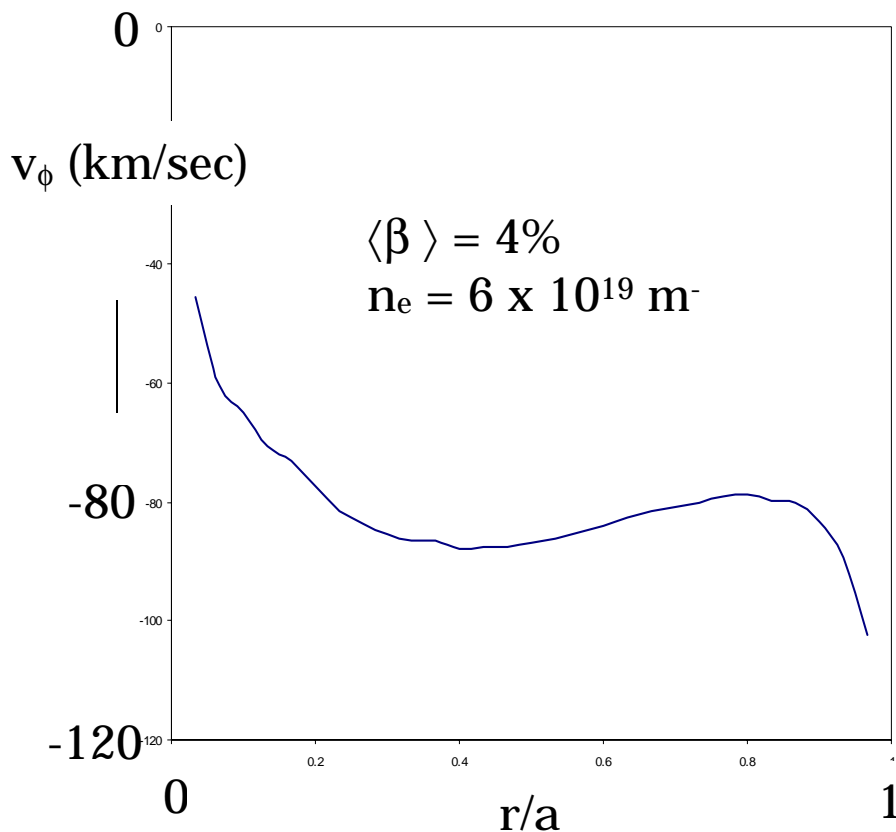
(Details in Physics Design Document)

| | case | β (%) | Loss of surfaces at edge (%) | Sum of effective island widths (%) | Total effective flux surface loss (%) |
|-------------------|-------|-------------|------------------------------|------------------------------------|---------------------------------------|
| Reference case | S3 | 4.1 | 0 | <1 | <1 |
| Vacuum cases | vac1 | 0 | 3.1 | <1 | 3.1 |
| | vac2 | 0 | 10.4 | <1 | 10.4 |
| | vac3 | 0 | 5.2 | <1 | 5.2 |
| | vac4 | 0 | <1 | <1 | <1 |
| | vac5 | 0 | 2 | <1 | 2.0 |
| Startup snapshots | t=50 | 1.2 | 6.2 | 3.8 | 10.0 |
| | t=100 | 3.4 | 0 | 10.1 | 10.1 |
| | t=116 | 3.7 | 0 | 5.5 | 5.5 |
| | t=139 | 3.9 | 11.4 | 1.2 | 12.6 |
| | t=303 | 4.6 | 0 | 2.5 | 2.5 |

- Expect further improvements using trim coils.

An Additional Effect: Plasma Flow Shields out Resonant Perturbations at Rational Surfaces

- Plays major role in reducing vulnerability of present day tokamaks to field errors.
- Tokamaks most vulnerable just before neutral beams turned on, when flow diamagnetic.



Predicted NCSX rotation frequency \approx
DIII-D cases where penetration threshold
studied with neutral beams turned on.

Strong flow driven by ambipolar E_r even
in absence of external momentum input.

Predicted resonant magnetic perturbation
penetration threshold \approx measured DIII-D
threshold with beams turned on.

($B_{rnm}/B \approx 6 \times 10^{-4}$ for $n \approx 6 \times 10^{19} \text{ m}^{-3}$)

Conclusions

- A new coil design code has been built around PIES and applied to NCSX. Coil design modified to heal flux surfaces, while preserving engineering and physics constraints.
- More accurate modeling of coil pack (using multiple filaments) improves calculated flux surfaces.
- Calculations for five different vacuum states and five snapshots during startup scenario find acceptable flux surfaces loss.
- Trim coils will provide additional flexibility.
- Strong ambipolar flow additionally predicted to shield out resonant perturbations.