NCSX

Design Basis Analysis

Stress Analysis of the NCSX Trim Coils

NCSX-CALC-133-001-00

14 May 2008

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I have reviewed this calculation and, to my professional satisfaction, it is properly performed and correct. I concur with analysis methodology and inputs and with the reasonableness of the results and their interpretation.

> **Reviewed by:** H.M. Fan

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1.0 Executive Summary

This documents the results of the stress analysis of the NCSX Trim Coils in support of the Final Design Review. It includes the coil conductor and encasing structure up to but not including the support brackets which tie them to the MCWF/TF/PF support structures.

Worse case running load were found to be 80 lb/in for the inner coils and 60#/in for the outer coils. This is driven by the TF field since the trim coils lie just inside the TF coils. All of the GRD scenarios resulted in running loads of 50#/in or less as a result partially of lower TF levels.

The analysis results show the current design to be acceptable. Conservative estimates of the reaction loads are provided as input to the bracket design and for MCWF/TF/PF interface evaluation.

2.0 Assumptions and Notable Concerns

The design is based on a 120 turn copper winding wrapped with CTD -101K insulation turn to turn insulation and groundwrap. The conductor is partially encased by mounting it to a ¾" 304SS base plate and capturing it with a 3/16" wall 304SS formed U-Channel along the straight legs of the coil and attached to the base plate with a 1/8" weld. The coils are supported off the MCWF/TF/PF supported structure with brackets attached to the base plate. Where the brackets attachments are made, welding of the U-Channels is not accessible and assumed free. There are 4 attachment points per inner trim coil, at or near the corners along the toroidal running legs and unsupported along the radial running legs. The outer trim coils are supported along each of the 4 legs at 2-3 locations each. The conductor is assumed to be free to slide within the case. Analysis was done with and without friction. The conductor is free to lift off along the unsupported corners.

Analysis includes the impact of thermal stresses due to the cool down based on a difference in CTE of 2.e-6 m/m-K over the temperature change of 220 K (300K-80K). It is assumed that cool-down is slow enough such that large thermal gradients are not generated between the coils and the MCWF/TF/PF supported structure. An allowable gradient between the structures has not been established.

3.0 Analysis

An ANSYS model was created using the basic geometry defined by the ProE models but simplified to capture significant features. Only the coil centerline geometry from the ProE model was imported into ANSYS. The cross section geometry was modeled parametrically in ANSYS and extruded for each coil. Welds are modeled as coupling between welded interfaces at the top of the U-Channel and base (top) plate. The conductor-case interface was modeled with contact elements. Coefficients of friction of 0 and 0.3 were assumed during the initial analysis to assess impact. The conductor is fully captured by the u-channels along the straight legs but only supported by the plate in the corners where it is free to lift off. The supports are not modeled explicated; only the location of the supports are captured with constraints in the model as shown in the figures below. Reaction loads at the constraints are supplied for use in support bracket and hardware calculations being done outside the scope of this report.

An electromagnetics model was augmented with field sources from the Modular, TF and PF coils taken from an existing model of the Integrated Structure generated by HM Fan. The EM model represents a full period and assumes cyclic symmetry. While this is not true in all cases since the trim coils will be used to correct non stellarator symmetric field errors so will have current distributions that are not stellarator or cyclic symmetric, the main coil fields are symmetric. The forces on the trim coils are dominated by the field

from the Modular, TF and PF coils while the self fields from the trim coils are comparatively small. The trim coils were assumed to carry their design current of 20 kAturns in all scenarios analyzed. The plot below shows the resultant field from all the coils for the 2T High Beta scenario at t=0.197s.

The running load on the trim coils was considered to be the best metric for identifying worse case scenarios to consider for detailed analysis since the response is driven by flexure of the coils between their supports. Alternatively the net force on the coils could have been used but this was not considered representative since there are large opposing forces in the coils. A scan of the expected operating scenarios given in the GRD and several additional flexibility requirements provided identified the worse case running load on the trim coils at their design current of 20 kA-t to be 80 lb/in for the inner coils and 60#/in for the outer coils. This is driven by the TF field since the trim coils lie just inside the TF coils. All of the GRD scenarios resulted in running loads of 50#/in or less as a result partially of lower TF levels.

The loads were checked with an independent FORTRAN code called forces5.f which was then used to scan thru all the GRD scenarios and time points plus additional physics flexibility cases. The results are tabulated below.

The forces on the coil are shown below for the iota=0.19 case which gave rise to the largest running load of 80 lb/in on the inner coils. The outer coils see a lesser value of 60 lb/in. The loads are greatest on the radial legs which cross the TF field and show the characteristic 1/r drop in magnitude.

Material properties for the coils and support are taken from the NCSX Online Material Database:

Trim Coils Material Properties

The conductor was modeled using equivalent properties calculated from a detailed flexural model of (previously) 121 turns with groundwrap. The model was simply supported and the ends and a unit load applied at the center. The flexural modulus was calculated as it would be for a flexural test setup:

$$
E_b = \frac{PL^3}{4bh^3 d_{max}}
$$

where

 P is the applied load L is the length of the test specimen b is the section width h is the section height dmax is the max deflection at load P

For verification, the model was rerun using the equivalent flexural modulus and displacements were checked to assure accurate stiffness representation.

Scaling factors for the copper and insulation stresses were determined by comparing max outer fiber stresses for the insulation in the initial model with the results achieved in the equivalent model. Similarly, max stresses at the copper were compared to their equivalent results. Unlike the insulation, the copper does not experience the extreme fiber stress in bending so its scale factor is further reduced based on distance from the neutral axis. Equivalently the copper stress can be normalize to the peak equivalent stress to determine the scale factor.

Equivalent Flexural Modulus and Stress Scaling for Trim Coils

Results

The model was run initially with just a single coil to study the relative impact of EM loads and Cool down loads, separately and combined, and to see the effect of the assumed coefficient of friction on the results. They were iterations in the design and analysis until converging on the present configuration.

The results show some sensitivity to the coefficient of friction but there is adequate margin at both extremes. The actual design now calls for potting of the conductor with the case which will make the mu=0 less appropriate. However, we cannot assume a fully bonded coil (which earlier results suggested would have more robust) since the corners are not captured and the conductor will very likely separate from the plate.

While the trim coils are all of only two type (inner and outer), the loading differs from coil to coil as do the details of the supports. The structural model was run with 8 trim coils (half period) to capture the peak stresses in any coil. The results tabulated below are for the iota=0.19 case (largest running load of 80 lb/in in a 'real' scenario)

The results above represent the peak stresses found in the model components. As the plots that follow will show, the primary stresses (ie averages thru sections) in the supporting structures (plate and U-Channel) are much smaller and are below the allowable of 140 MPa for 304 SS. For EM Only, the stresses are well within the limits for Local Primary and Primary plus bending of 210 MPa. For Cool down and Cooldown plus EM, the allowable is 420 MPa, governed by the Total primary plus secondary (thermal) stress limit. Once again the stresses are shown to be less than the allowable.

Metallic Structure Acceptance Criteria

The figures below show stress distributions in the full set of coils. What is apparent is that the average stresses are fairly low (plots are very blue). The peaking is in the conductor corners and at the end of the welds that attach the u-channels to the support plate.

Plot of Coil Assembly Von Mises Stresses

Plot of Conductor Von Mises Stresses (note: equivalent stresses)

The conductor plots show modest stresses where it is captured by the u-channel. At the corners where it is free, bending is greatest. The stresses are scaled by factors presented earlier to give the max insulation and copper stresses in the conductor tabulated above.

Plot of base (top) plate Von Mises Stresses

Plot of U-Channel Von-Mises Stresses

The ANSYS plots show high peak stresses at the end of the weld due to the geometric discontinuity there. Generally accepted practice is to look at averaged stresses over the local region to compare to allowable stress limits or for fatigue evaluation purposes.

Within ANSYS this is done by looking at element average stresses as opposed to the peak node stresses normally plotted. The plots below compare the differences. In the region of high stress the averaging makes a significant difference. In regions where the gradients are small, the averaging has little impact.

Plot of Peak Stress Region at Weld in U-Channel. Node stress still meets Acceptance critera

Two additional load cases were run thru the EM and Structural Analysis: the 0.5T TF only case which showed similarly high running loads of 80 lb/in and the 2T high beta scenario which has driven the design of the MCWF/TF/PF support structures. The node stress results are tabulated below:

While not shown here, the peak stresses found above occur in similar locations as the earlier case – at the end of welds of the u-channel to the base plate. An examination of the average element stresses for the 0.5T TF case shows the peak stress drops from 21.7 ksi to 8.2 ksi. Also the actual channel geometry show the U extending beyond the plate

which will further reduce the node stresses show. Regardless, the node stress is still with the allowable for 304 SS (1.5 K Sm=30 ksi for local primary or primary plus bending).

The maximum shear stress in the insulation was extracted from the model by first tabulating the principle stresses (s1, s2, s3) and computing the max shear stress as the max(abs(s1-s2)/2, abs(s2-s3)/2, abs (s3-s1)/2). From the detailed model of the conductor the scaling factors for shear stress were found to be equal to the scale factor for bending (ie 0.25). The max shear for the worse case scenario below is $0.25*14 = 3.5 \text{ MPa}$ (0.5 ksi) well within the capability of the insulation.

The reaction loads were extracted for the iota=0.19 scenario for use in bracket analysis. The table below provides the detailed results for each bracket location. Results are given in the global coordinate system (z vertical) for the four corner supports on the inner trim coils and along the four legs of the outer coils. The results show that the initial assumptions of designing the brackets to carry 80 lb/in over 1 leg of the coil $(-28" \text{ long})$ gave a reason approximation the max load encountered. While the EM component is actually smaller, the cool down does add a fair amount of load.

Reaction Forces at Trim Coil Support Brackets

iota=0.19 scenario (with max running load of 80#/in)

Previous estimate based on 80#/in over ~28" **2240** lb

The location of the supports tabulated above is shown in the figure below:

Additional results and information can be found in the attached presentation material prepared in support of the Trim Coil Final Design Review.

4.0 Summary & Commentary

The analysis herein will be used to finalize the selection of materials and welds (base plate to U-channel and the connections to the TF brackets) for the trim coils. Based on the results, it appears that 304 SS is acceptable for both the plate and the U-channel. The stresses in trim coils conductor, insulation and encasing structure are shown to be within their allowables. The reaction loads provided will be applied to the global structural model as part of a separate analysis.

1 Trim Coils Final Design Review Supporting Stress Analysis Art Brooks 5 May 2008

Force Scan Done with FORTRAN Code Benchmarked with ANYS

