

# COIL FLEXIBILITY AND PROFILE ROBUSTNESS

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NCSX Physics Validation Review  
March 26-28, 2001  
Princeton Plasma Physics Laboratory

# OUTLINE

To achieve the scientific goals of the NCSX mission, the NCSX device must be capable of supporting a wide range of variations in plasma configuration about the reference baseline equilibrium.

- We will demonstrate the flexibility of NCSX coils to support such configuration variations,

and

- Demonstrate the robustness of performance of NCSX plasmas for substantial variations about reference design values of the plasma current, beta, and profile shapes.

# NCSX COIL SYSTEM

## Modular coilset M1017

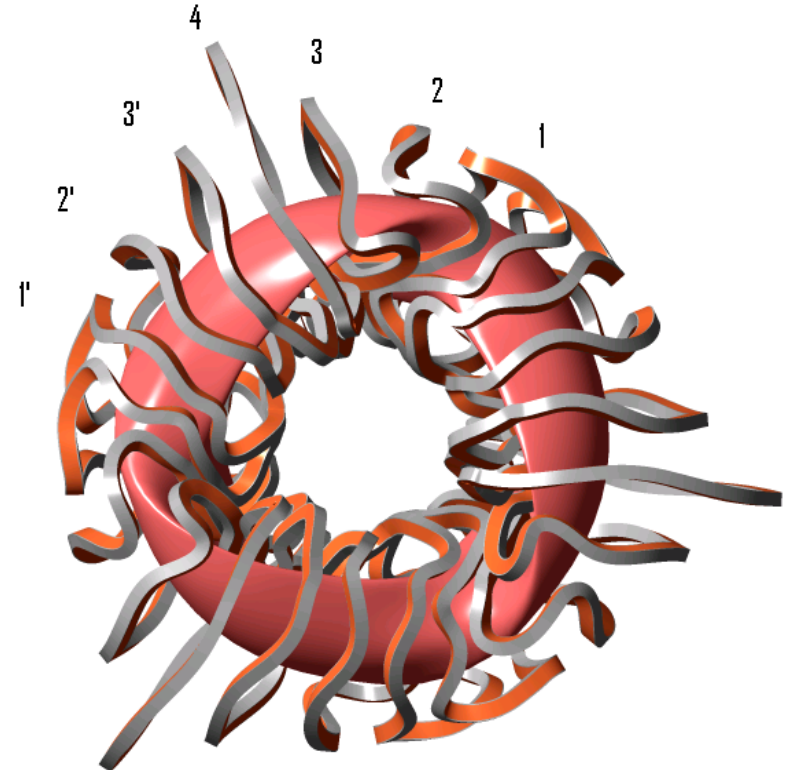
- 4 independent coil currents  
(independent coils labelled 1, 2, 3, 4)

## Auxiliary TF coils

- provide  $\pm 0.3$  T at R=1.4 m

## Axisymmetric PF coils

- provide at least 4 lowest order multipoles



## COMPUTATIONAL TOOLS

**STELLOPT** – a VMEC based free-boundary optimizer which varies coil currents to target configurations with good physics:

- Stable to Kink and Ballooning modes
- Good quasi-axisymmetry (QA)

Essential code modules within STELLOPT are:

**VMEC**<sub>(Hirshman)</sub> => Equilibrium,

**TERPSICHORE**<sub>(Cooper)</sub> => Kink evaluation (incl. modes with  $n$  up to  $n_{\max} = 7$ )

**COBRA**<sub>(Sanchez)</sub> => Ballooning evaluation,

**NEO**<sub>(Kermbichler)</sub> => QA-ness measured by effective helical ripple,  $\epsilon_h$ .

# PLASMA PERFORMANCE AS $\beta$ AND $I_p$ ARE VARIED

## Question:

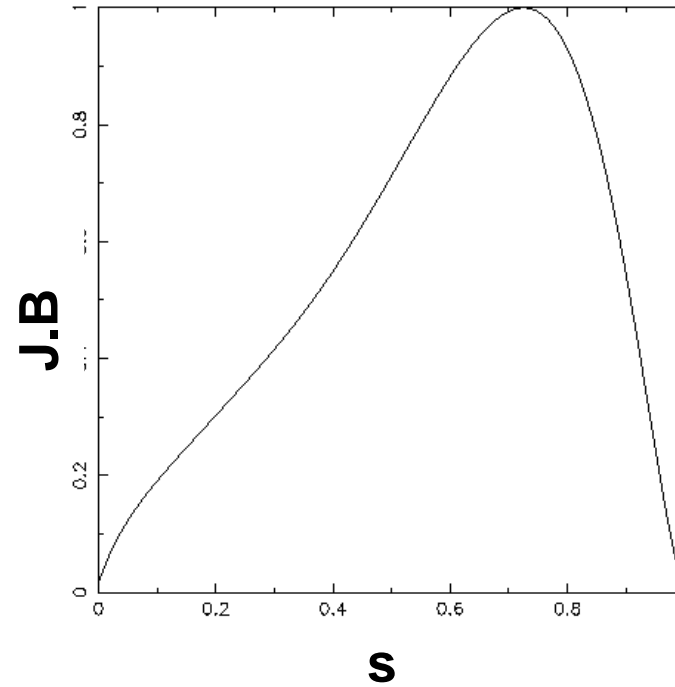
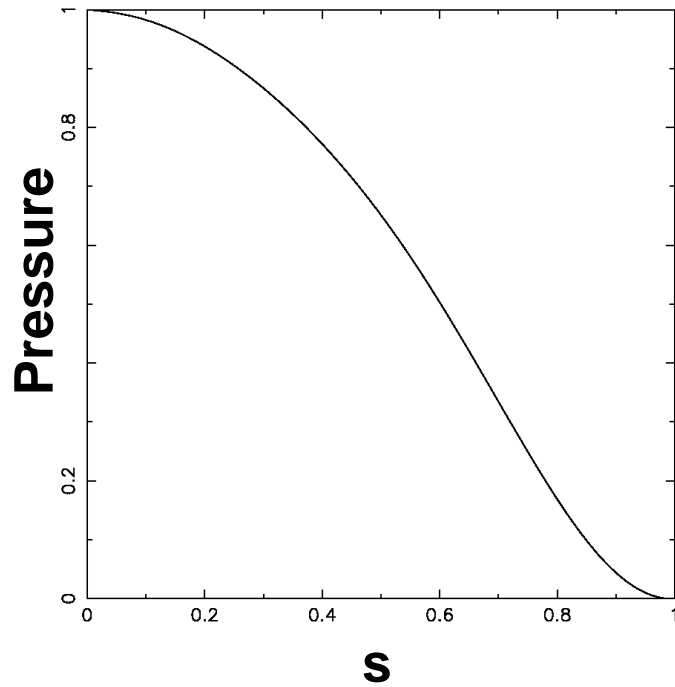
- Can coil currents be found which produce stable plasmas with good QA as  $I_p$  and  $\beta$  are varied from their reference values?
- Are there stable paths from S1 states with  $I_p = 0$  kA,  $\beta = 0\%$  to S3 states with  $I_p = 174$  kA,  $\beta=4\%$ , or states at full current with even higher  $\beta$ ?

## Answer:

- YES! – Using reference P(s) and J.B(s) profiles, stable configurations with low  $\varepsilon_n$  are found over a wide region of the  $I_p - \beta$  plane, including a stable configuration at  $\beta = 5\%$ .

# 'REFERENCE PROFILES' FOR $I_p - \beta$ SCAN

(and about which variations will be made)



## **$I_p - \beta$ SCAN RESULTS ( $B_T = 1.7$ T)**

$\beta$ [%]	0.0	1.0	2.0	3.0	4.0	5.0
$I_p$ [kA]						
43.5		$\epsilon_h = 2.11\%$	$\epsilon_h = 1.30\%$	$\epsilon_h = 1.30\%$	$\epsilon_h = 0.86\%$	
87		$\epsilon_h = 1.56\%$	$\epsilon_h = 1.60\%$	$\epsilon_h = 1.28\%$	$\epsilon_h = 0.86\%$	
130.5		$\epsilon_h = 0.77\%$	$\lambda_0^K = -6.0e-5$ $\lambda_1^K = -2.7e-5$ $\epsilon_h = 0.84\%$	$\lambda_0^K = -8.8e-6$ $\lambda_1^K = -2.2e-5$ $\epsilon_h = 1.14\%$	$\epsilon_h = 0.67\%$	
174	$\epsilon_h = 0.79\%$	$\lambda_0^K = -1.9e-5$ $\lambda_1^K = -2.0e-5$ $\epsilon_h = 0.81\%$	$\lambda_0^K = -2.3e-5$ $\lambda_1^K = -2.3e-5$ $\epsilon_h = 1.43\%$	$\epsilon_h = 0.79\%$	$\epsilon_h = 1.29\%$	$\epsilon_h = 1.66\%$

- **Blue boxes** => Kink and Ballooning modes are stable at that  $I_p, \beta$ .
- **Red boxes** => Kink unstable with small  $\lambda^K$ , but ballooning stable.

NOTE: Config with  $I_p = 174$  kA,  $\beta = 5.0\%$  is stable!

(Stable plasmas with  $\beta$  up to 6.5% have been found for the M0907 coilset)

## • SUMMARY OF $I_p - \beta$ SCAN RESULTS

- 14 of 18 optimized configurations with different  $I_p$ ,  $\beta$  values were stable w.r.t. kink and ballooning modes.
- The remaining 4 configurations were stable to ballooning modes and had small kink eigenvalues. Re-optimization with adjusted weights will probably stabilize these cases.
- Each configuration is marginally stable at the given  $I_p$ ,  $\beta$  ( $\Rightarrow$  configurations with low  $\beta$ -limits are easily dialled).
- In all cases, good QA-ness was obtained, measured by effective ripple amplitudes,  $\varepsilon_h < 1.5\%$  at  $s = 0.5$ .
- A stable configuration at  $\beta = 5\%$  was found with  $I_p = 174$  kA and  $B_T = 1.7$  T.
- Modular coil currents vary  $< \pm 15\%$  over the  $I_p - \beta$  plane.  
 $B_T^{\text{Aux}}$  varies  $< \pm 0.10$  T.



# PLASMA PERFORMANCE AS PROFILES ARE VARIED

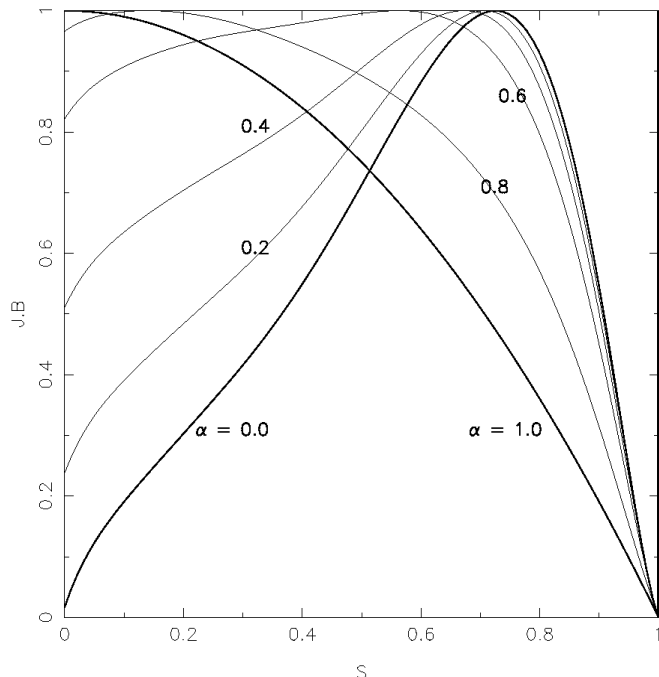
## Question:

- What happens to plasma performance ( $\beta$ -limits, QA measure  $\varepsilon_h$ ) when plasma profiles are varied about reference forms at fixed  $I_p$ ,  $B_T$ ?
- Is the reference configuration sitting atop a pinhead optimum so that as the profiles are varied the performance drops off a cliff?

## Answer:

- **NO!** – We find configurations with a wide range of current and pressure profiles which have  $\beta$ -limits in excess of 3.0% and which have good QA.

# CURRENT PROFILE VARIATION IN CORE REGION



## Question:

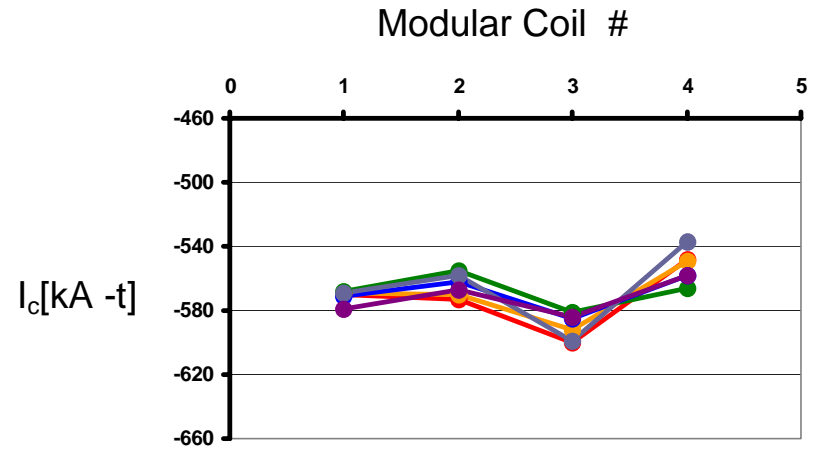
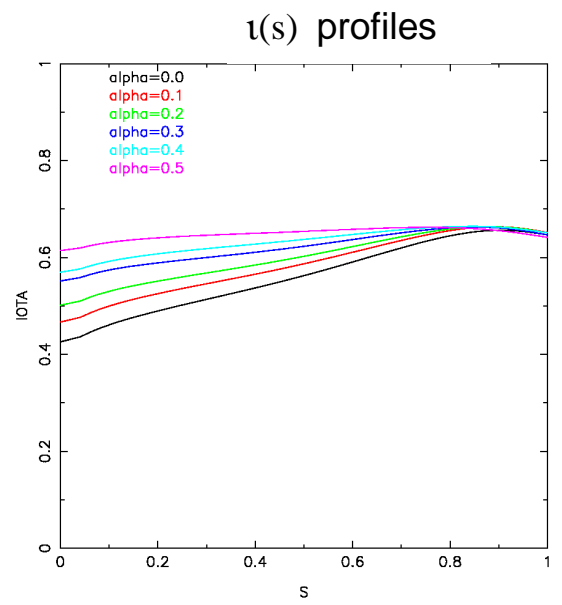
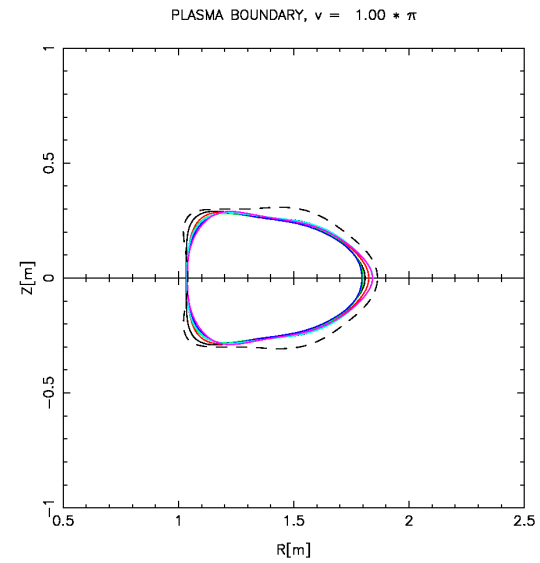
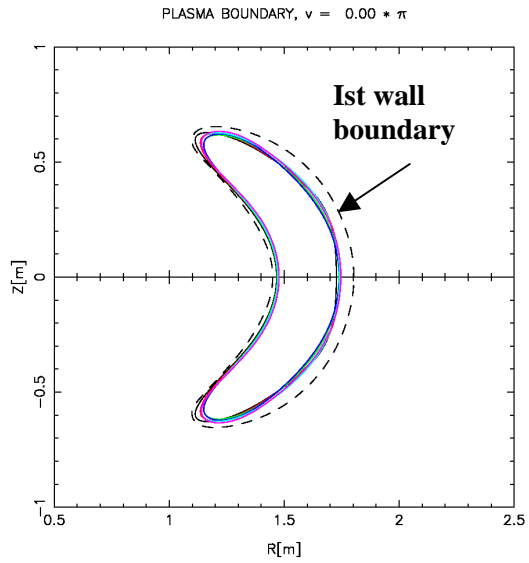
- Using the reference  $p(s)$ , and  $I_p = 174$  kA,  $B_T = 1.7$  T, for what range of J.B profiles can we find stable configurations with  $\beta \geq 3.0\%$ ?

## Answer:

- Stable range is  $0 \leq \alpha \leq 0.5$ .
- Stable profiles have  $\varepsilon_h \leq 1.3\%$  at  $s=0.5$ :

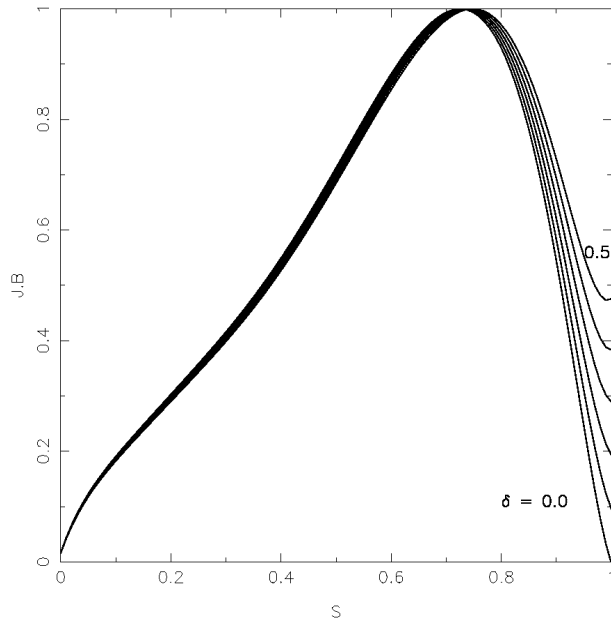
$\alpha$	0.0	0.1	0.2	0.3	0.4	0.5	0.6	0.7
$\lambda_0^K$	S	S	S	S	S	S	$-7.3e-4$	$-9.1e-4$
$\lambda_1^K$	S	S	S	S	$-1.5e-5$	$-2.8e-5$	$-5.1e-5$	$-8.0e-5$
$\lambda_B$	S	S	S	S	S	S	S	S
$\varepsilon_h[\%]$	1.29	1.16	0.90	0.88	1.32	1.27	1.13	1.05

# Plasma Boundaries for $J.B^{core}$ variation with $\beta=3.0\%$



Loss of stability for  $\alpha > 0.5$  possibly due to loss of shear.

# CURRENT PROFILE VARIATION IN EDGE REGION



## Question:

- What happens to plasma performance when  $J.B$  is made finite at the plasma edge?
- Use coil currents from the  $I_p=174$  kA,  $\beta=5.0\%$  configuration obtained in the  $I_p - \beta$  scan.

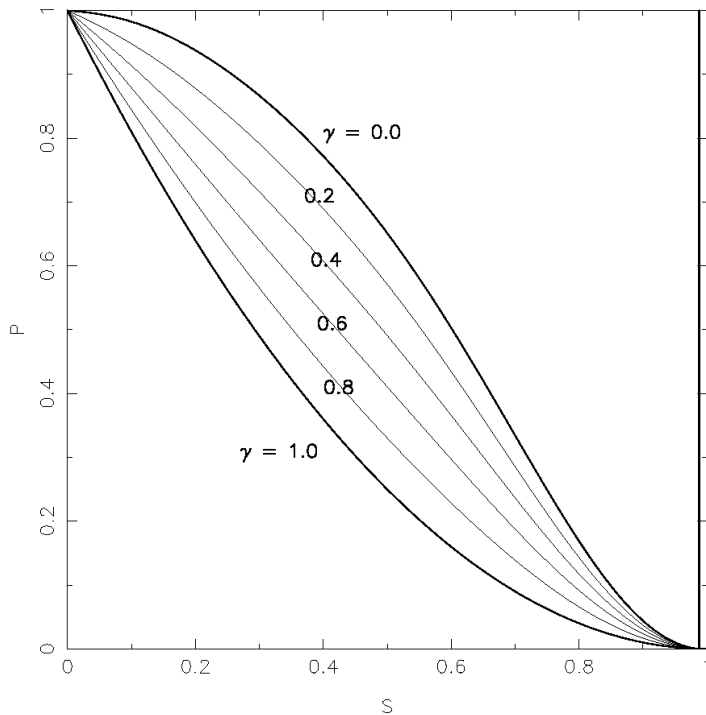
## Answer:

- Keeping  $\beta=5.0\%$  as a target for all configurations in the scan, the configurations remains stable even as  $J.B^{\text{edge}}/J.B^{\text{max}}$  is raised to 50%!

- **Contrast with Tokamak behavior.**
- **H-mode profiles may be beneficial to NCSX.**

M.I. Mikhailov, V.D. Shafranov  
"Stable Current Profile in a Stellarator with Shear",  
Nucl. Fusion **30**, 413 - 421 (1990).

# PRESSURE PROFILE VARIATION



- By how much can we peak the  $p(s)$  and maintain stable configurations with good QA at  $\beta = 3.0\%$ ?
- Use reference J.B and the pressure profiles shown.
- Stable range of pressure profiles is  $0 \leq \gamma \leq 0.8$ . (with  $\gamma=1.0$  stable at  $\beta = 2.5\%$ ).

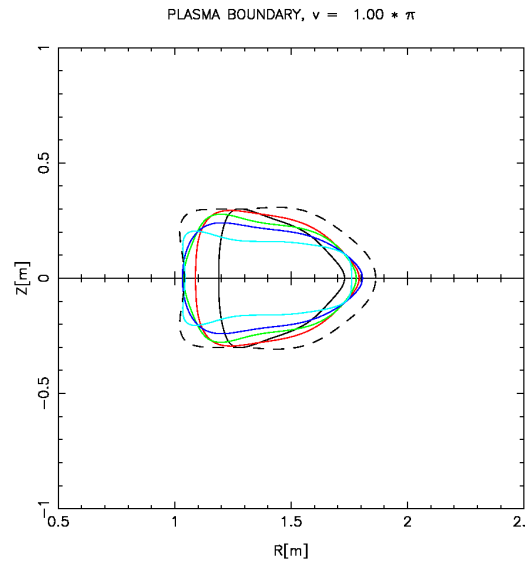
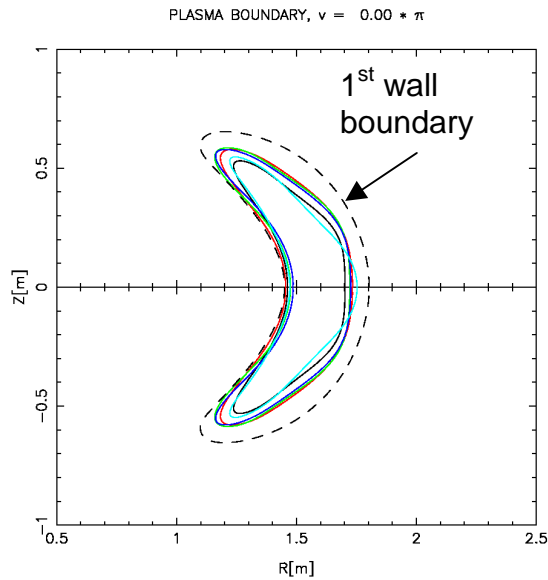
$\gamma$	0.0	0.2	0.4	0.6	0.8	1.0
$\lambda_0^K$	S	S	S	S	S	$-3.0e-4$
$\lambda_1^K$	S	S	S	S	S	$-5.4e-5$
$\lambda_B$	0	0	0	$0^*$	$0^*$	$0^*$
$\epsilon_h[\%]$	0.80	0.72	0.78	1.05	0.73	0.62

- Low  $\epsilon_h$  values obtained in almost all cases.
- Max coil current variation  $\sim 50$  kA (Modulars 3 and 4).

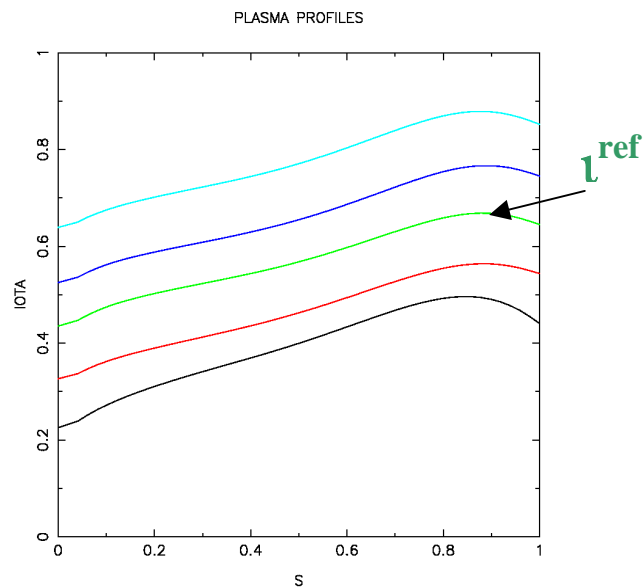
# FLEXIBILITY TO CONTROL EXTERNAL TRANSFORM

- Will be an important control knob in the experiment
  - can be used to test importance of avoiding low order rational surfaces in the plasma region.
  - is a means of controlling discharge evolution.
- We demonstrate the capability of NCSX coils to effect substantial changes in the external field contribution to  $\iota(s)$ .
- Flexibility experiments shown here assume fixed  $B_T$  and  $I_p$ , and induce  $\Delta\iota$  by causing appropriate changes in plasma shape.

# FLEXIBILITY TO CHANGE $\iota(s)$ AT FIXED $I_p$ , $B_T$

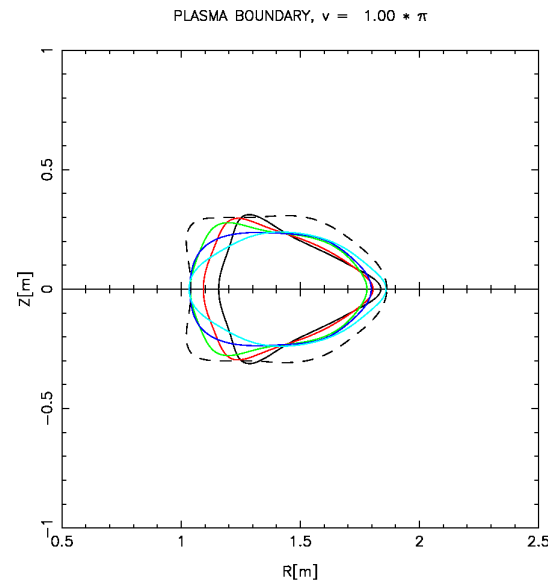
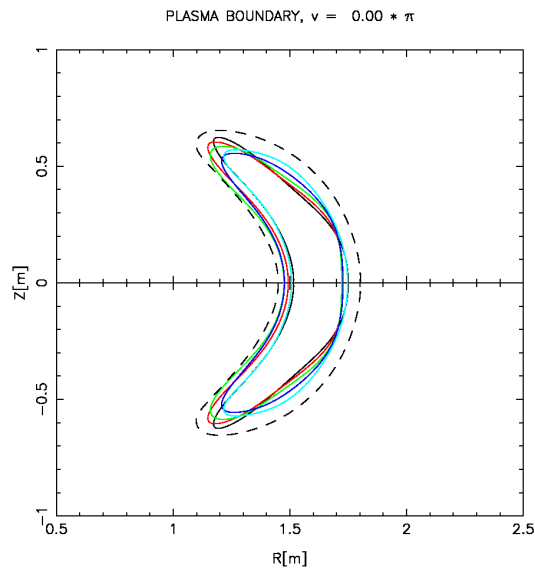


- $I_p = 174$  kA,  $B_T = 1.7$  T
- $\beta = 0\%$

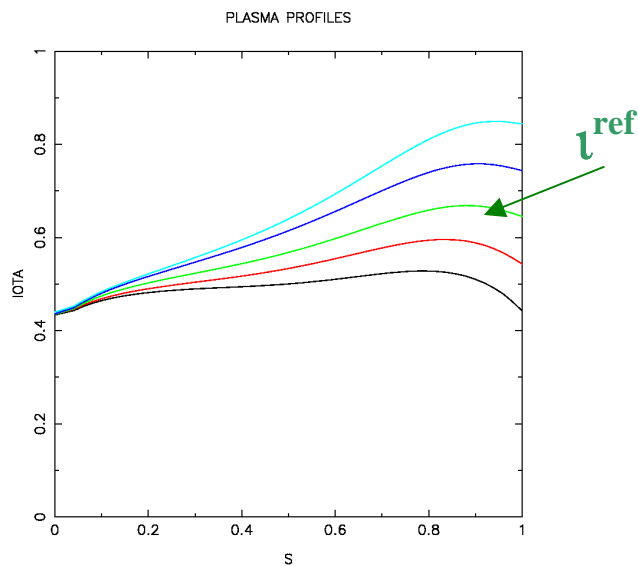


- raise/lower  $\iota(s)$  at constant shear.
- $\Delta\iota = \pm 0.2$  is possible:  
~50% of  $\iota^{ref}(0)$ , ~30% of  $\iota^{ref}(1)$ .
- For  $\Delta\iota = +0.2$ , coil currents vary ~120 -150 kA-t (all coils).
- Max  $B_T^{Aux} \approx -0.1$  T, for  $\Delta\iota = +0.2$

# FLEXIBILITY TO CONTROL SHEAR AT FIXED $I_p$ , $B_T$



- $I_p = 174$  kA,  $B_T = 1.7$  T
- $\beta = 0\%$



- raise/lower  $\iota(1)$  at fixed  $\iota(0) = 0.45$
- $\Delta\iota(1) = \pm 0.2$  is possible  
( $\iota^{\text{ref}}(1) = 0.65$ )
- For  $\Delta\iota(1) = \pm 0.2$ ,  $\Delta I_c^{\text{Mod. 4}} \approx 80$  kA-t  
(others less)
- Max  $B_T^{\text{Aux}} \approx +0.4$  T, for  $\Delta\iota(1) = -0.2$



## FLEXIBILITY TO VARY QA-NESS

- The ability to generate configurations with good QA is an essential requirement for NCSX.
- For a systematic exploration of the role of QA in improving the transport properties of stellarator plasmas it is necessary to have the ability to control the degree of QA-ness.

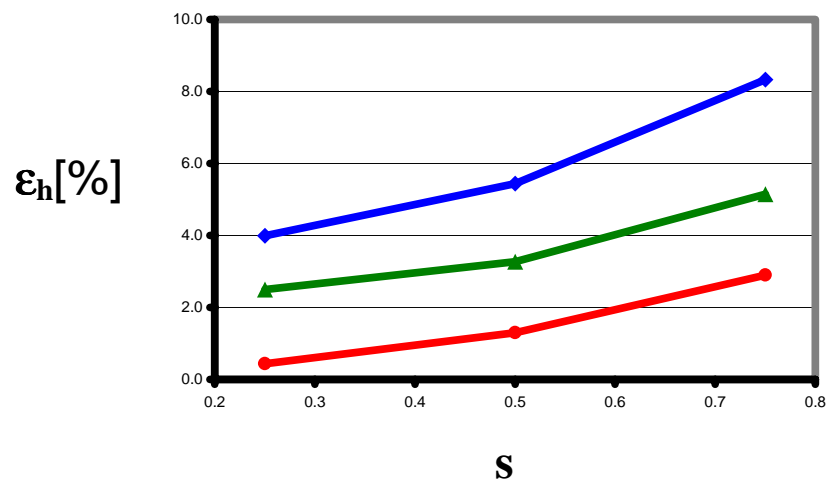
### Question:

- Do we have QA control while maintaining plasma stability?

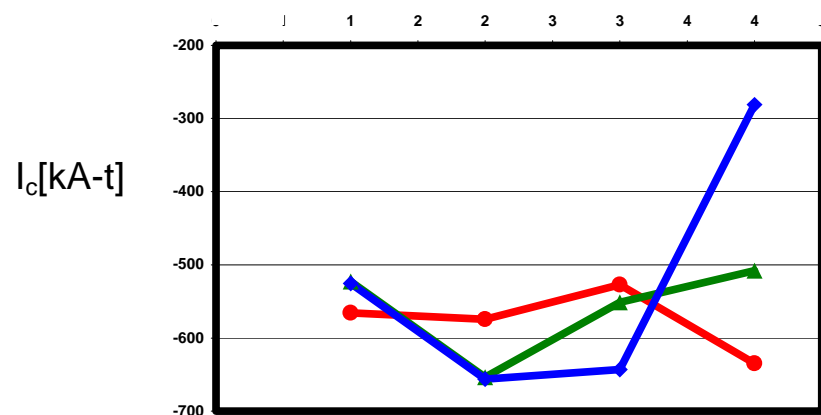
### Answer:

- YES!

## FLEXIBILITY TO VARY QA-NESS



Modular Coil #



- 3 configurations, each with  $I_p = 43.5$  kA,  $\beta = 3.0\%$ .
- Among configurations  $\epsilon_h$  varies by a factor of 9 at  $s=0.25$  ( $r/a \approx 0.5$ ), and factor of 4 at  $s=0.5$ .
- Each configuration is stable to kink and ballooning modes
- To obtain case with highest  $\epsilon_h$ , the  $I_c$  for modular coil 4 was artificially fixed at  $-281$  kA.
- Yet the kink and ballooning modes were able to be stabilized using just 3 coils!

# FLEXIBILITY TO EXPLORE STABILITY BOUNDARIES AND 3D SHAPE STABILIZATION

- Each stable free-boundary configuration in the  $I_p$  -  $\beta$  scan lies at a point of marginal stability w.r.t. kink and ballooning modes for the given profiles.
- To illustrate the type of experiment that can be run on NCSX aimed at understanding the physics that determines stability boundaries, consider two configurations from the  $I_p$  -  $\beta$  scan:

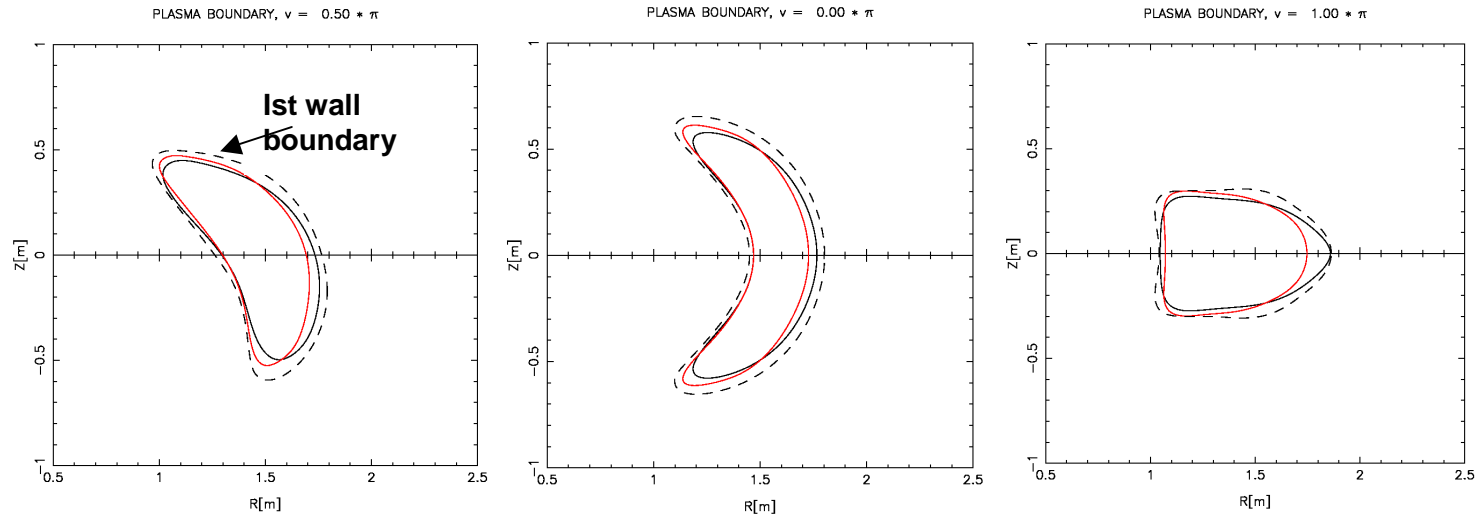
**C1**

$I_p = 43.5$  kA,  $\beta = 1.0\%$       and

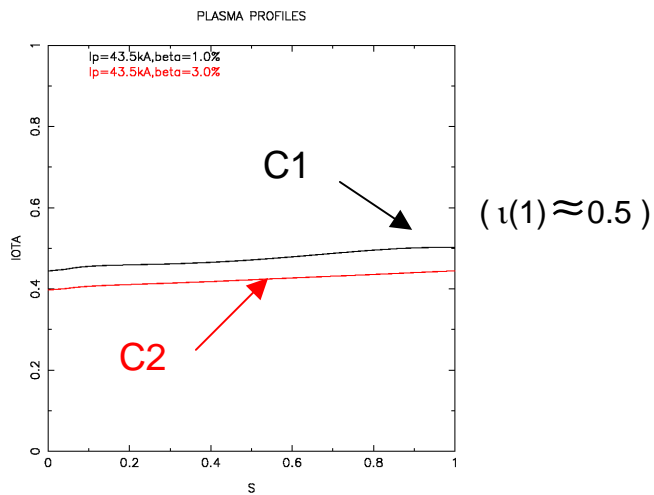
**C2**

$I_p = 43.5$  kA,  $\beta = 3.0\%$

# EXAMPLE OF 3D SHAPE STABILIZATION



C1 (black)  
C2 (red)

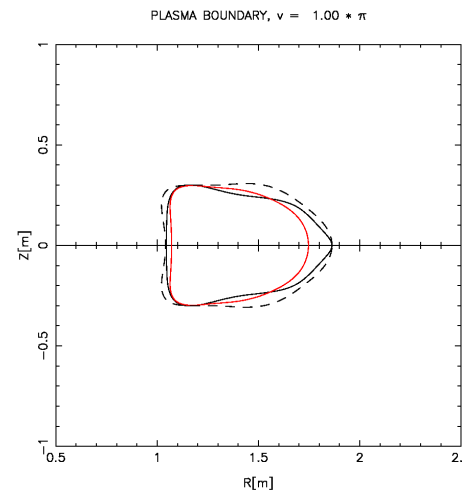
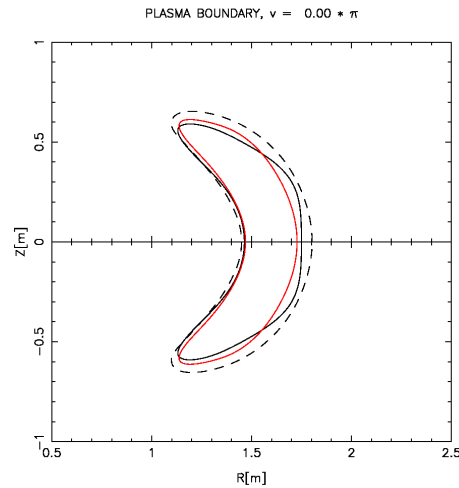
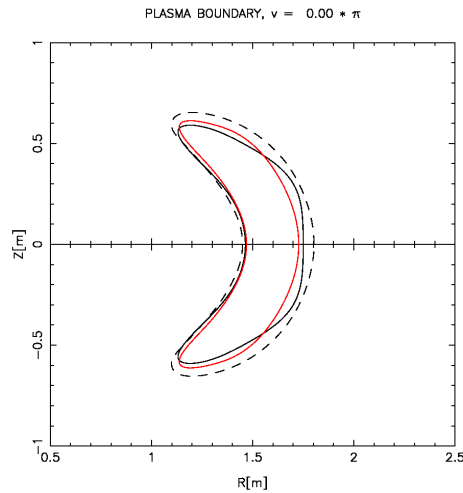


$\beta_{\text{Lim}} = 1.0\%$  for C1

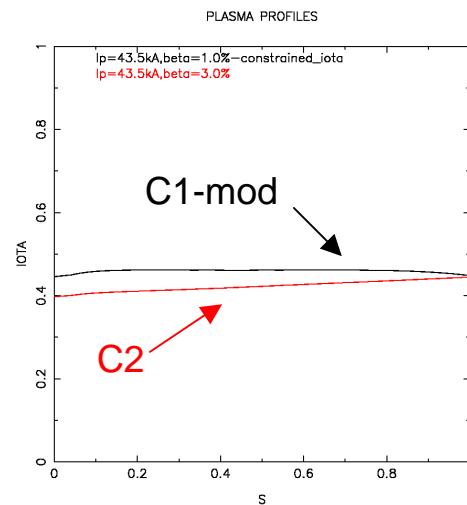
$\beta_{\text{Lim}} = 3.0\%$  for C2

- Difference in  $\beta$ -limits is due to difference in shape.

# REMOVE AMBIGUITY OF ROLE OF $\iota(1) \approx 0.5$

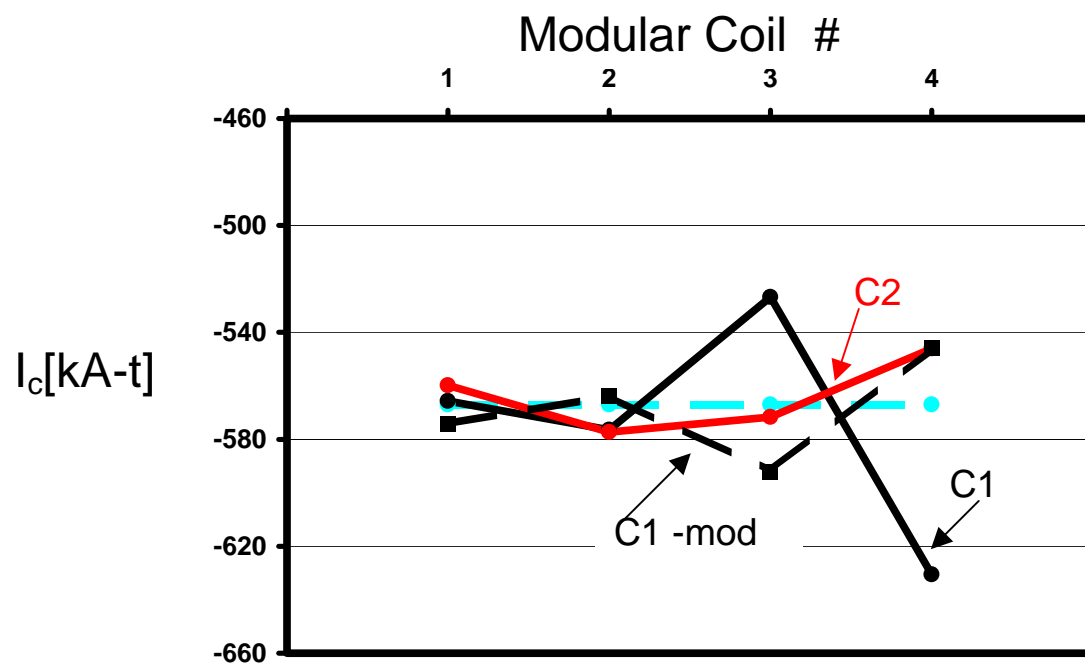


C1-mod (black)  
C2 (red)



- Impose  $\iota$ -control on C1 to produce new configuration, C1-mod, whose  $\beta$ -limit is 1.0%, but which has the same  $\iota_{\text{edge}}$  as the  $\beta_{\text{Lim}} = 3.0\%$  configuration.

## MODULAR COIL CURRENTS FOR THE 3D SHAPE STABILIZATION 'EXPERIMENTS'

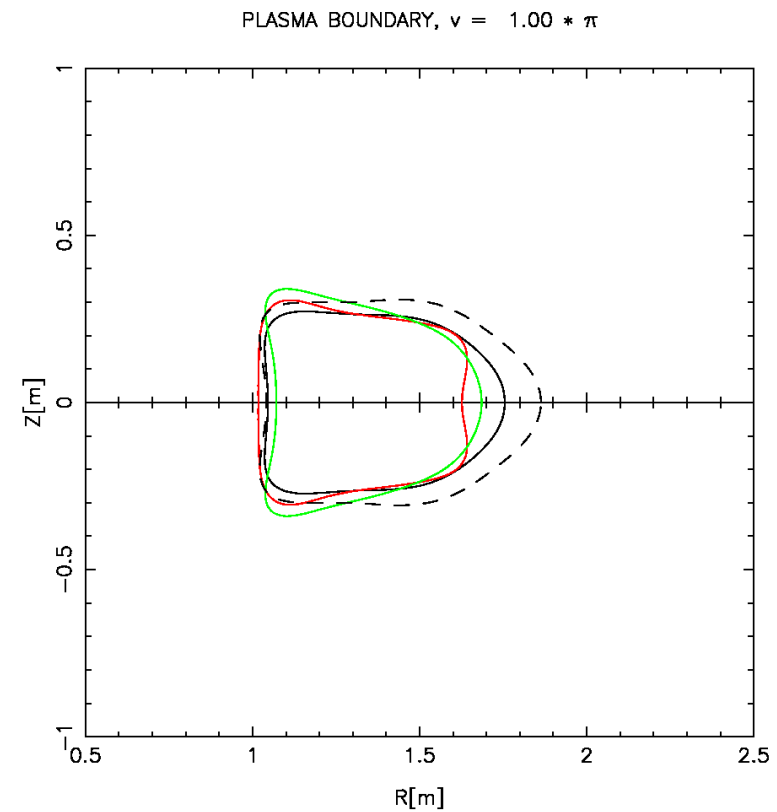
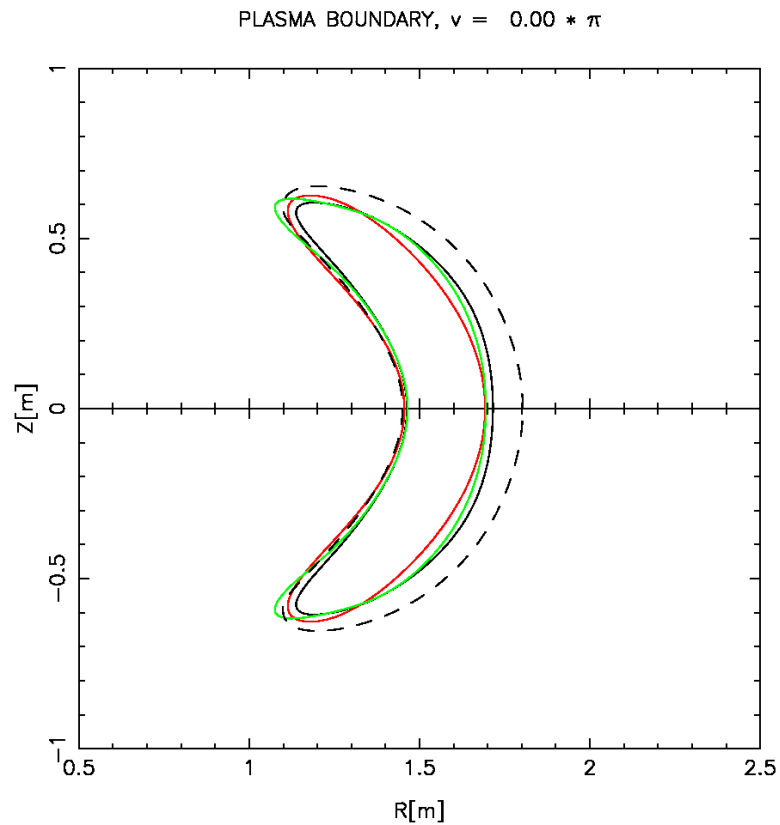


- Max  $\Delta I_c$  variation = 10%  
=> controllable.

## SUMMARY

- The performance ( $\beta$ -limits, QA-ness measure  $\varepsilon_h$ ) of NCSX plasmas is robust w.r.t. substantial variations of  $I_p$  and profile shapes about reference design values.
- The NCSX coil system has considerable flexibility to support the wide variety of experiments required by the NCSX mission.

# SUPPLEMENT-1: EFFECT OF $\beta$ and $I_p$ QUENCHES

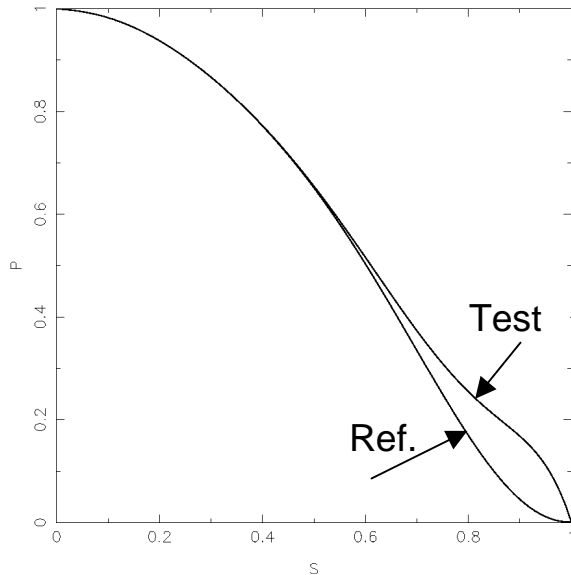


Black:  $I_p = 174$  kA,  $\beta = 4.2\%$    Red:  $I_p = 174$  kA,  $\beta = 0.0\%$    Green:  $I_p = 0$  kA,  $\beta = 4.2\%$   
Max. Inward radial shifts:  $\Delta R_{\min} = 2.2$  cm    $\Delta R_{\min} = 4.7$  cm



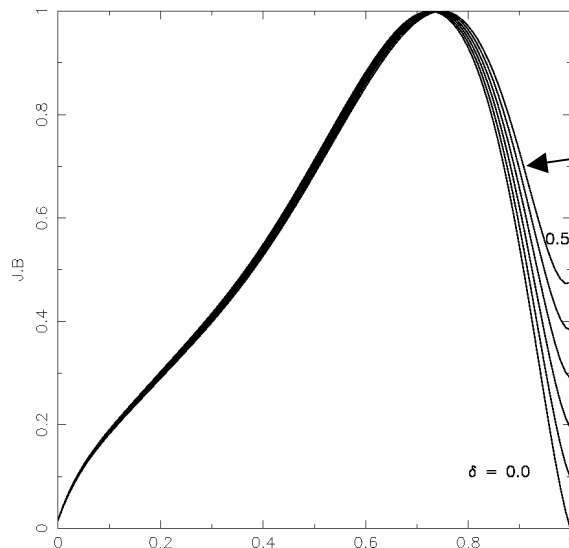
# SUPPLEMENT-2: EFFECT OF PRESSURE PEDESTAL ON STABILITY

-The road to H-mode profiles.



- “Test” pressure profile with finite edge gradient is stable at  $\beta = 4.0\%$ .

$$I_p = 174 \text{ kA}, B_T = 1.7 \text{ T}$$



Used this current profile (50% edge current density)